

Roll No.

Y – 3187

M.A./M.Sc. (Fourth Semester) EXAMINATION, May/June-2021

MATHEMATICS

Paper – 412

SPECIAL FUNCTIONS

Time : Three Hours

Maximum Marks : 85

Minimum Pass Marks : 29

Note—Attempt *all* questions.

Unit-I

1. (a) Evaluate 17

$$\Gamma' \text{ and } \frac{\Gamma(1/2)'}{\Gamma(1/2)}$$

- (b) State symmetrical property of Beta function and prove it. 17

Unit-II

2. State and Prove Integral formula for Hypergeometric function. 17

Unit-III

3. State and prove Dixon's theorem. 17

Unit-IV

4. State and Prove Rodrigue's formula for $P_n(x)$ and using this formula obtain the value of $P_4(x)$ at $n = 1$ 17

Unit-V

5. Prove that for Hermite polynomial 17

$$H_n''(x) - 2xH_n'(x) + 2nH_n(x) = 0$$

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