

Roll No. ....

**Y – 3181**

**M.Sc. (Mathematics) Fourth Semester EXAMINATION,**

**May/June-2021**

Paper – 402

**ADVANCED FUNCTIONAL ANALYSIS**

*Time : Three Hours*

*Maximum Marks : 85 (For Regular Students)*

*Minimum Pass Marks : 29*

*Maximum Marks : 100 (For Private Students)*

*Minimum Pass Marks : 34*

**Note**—Attempt *all* questions.

**Unit-I**

1. Let  $T$  be a contraction mapping defined on a complete metric space  $X$ , then prove that  $T$  has a unique fixed point. 17/20

**Unit-II**

2. If  $M$  is a closed linear subspace of a Banach space  $X$  then prove that  $X/M$  is a Banach space under the quotient form. 17/20

**Unit-III**

3. Explain normable and metrizable topological vector spaces. 17/20

**Unit-IV**

4. State and prove open mapping theorem for Frechet space. 17/20

**Unit-V**

5. State and prove Krein Milman's theorem. 17/20

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